

# Direct Torque Control of Induction Motor using Space Vector Modulation

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*Publishing Date: November 04, 2015*

## Abstract

A novel technique of controlling induction motor, called direct torque control, which controls both torque and flux directly and independently, is the topic of this work. In this work a control scheme for speed regulation based on the stator flux control in the stator reference frame using direct control of inverter switching has been adapted. The speed of induction motor is controlled by varying the stator flux through a PI flux controller. The validation of the MATLAB code is carried out using a typical induction motor drive details available from reference [1]. In the present investigations, the desired speed is set at 0.9 per unit. The initial value of the stator flux is set at 0.8 per unit. By varying the proportional gain, integral gain and integral time constant attempt is made to obtain the best response for speed, stator flux, torque, and d-q axis stator flux of the motor.

**Keywords:** Induction Motor, Vector Control, DTC.

## Introduction

Direct torque control (DTC) is one of the most excellent control strategies of torque control in induction machine. It is considered as an alternative to the field oriented control (FOC) or vector control technique. These two control strategies are different on the operation principle but their objectives are the same. They aim to control effectively the torque and flux. Torque control of an induction machine based on DTC strategy has been developed and a comprehensive study is present in this research. Induction machine have provided the most common form of electromechanical drive for

industrial, commercial and domestic applications that can operate at essentially constant speed. Induction machines have simpler and more rugged structure, higher maintainability and economy than DC motors. They are also robust and immune to heavy loading. Basically, there are two types of instantaneous electromagnetic torque-controlled AC drive used for high performance applications which are:

- **Vector Control (VC):** Based on stator current control in the field rotating reference frame.
- **Direct Torque control (DTC):** based on stator flux control in the stator fixed reference frame using direct control of the inverter switching.

## Principle of Vector Control

To explain the principle of vector control, an assumption is made that the position of the rotor flux linkages phasor,  $\lambda_r$ , is known.  $\lambda_r$  is at  $\theta_f$  from a stationary reference,  $\theta_f$  is referred to as field angle hereafter, and the three stator currents can be transformed into q and d axes currents in the synchronous reference frames by using the transformation

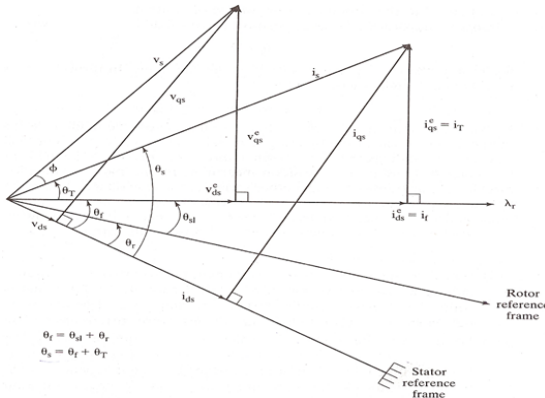
$$\begin{bmatrix} i_{qs}^e \\ i_{ds}^e \end{bmatrix} = \frac{2}{3} \begin{bmatrix} \sin\theta_f & \sin\left(\theta_f - \frac{2\pi}{3}\right) & \sin\left(\theta_f + \frac{2\pi}{3}\right) \\ \cos\theta_f & \cos\left(\theta_f - \frac{2\pi}{3}\right) & \cos\left(\theta_f + \frac{2\pi}{3}\right) \end{bmatrix} \quad (1)$$

From which the stator current phasor,  $i_s$ , is derived as

$$I_s = \sqrt{\left( (i_{qs}^e)^2 + (i_{ds}^e)^2 \right)} \quad (2)$$

$$\Theta_s = \tan^{-1} \left\{ \frac{i_{qs}^e}{i_{ds}^e} \right\} \quad (3)$$

The current phasor  $i_s$  procedure the rotor flux  $\lambda_r$  and the torque  $T_e$ . The component of current producing the rotor flux phasor has to be in phase with  $\lambda_r$ . Therefore, resolving the stator current phasor along  $\lambda_r$  reveals that the component  $i_f$  is the field-producing component, shown in Fig. 1.



**Figure 1: Phasor Diagram of the Vector Controller**

### Direct Vector Control in Stator Reference Frames with Space-Vector Modulation

The direct torque control method uses feedback control of torque and stator flux, which

are computed from the measured stator voltage and currents. As the method does not use a position or speed sensor to control the machine and uses its own electrical output currents and resulting terminal voltages, this is also referred as a direct self-control scheme. The method uses a stator reference model of the induction motor for its implementation, thereby avoiding the trigonometric operations in the coordinate transformation of the synchronous reference frames. This is one of the key advantages of the control scheme.

The stator q and d axes flux linkages are

$$\lambda_{qs} = \int (V_{qs} - R_s i_{qs}) dt \quad (4)$$

$$\lambda_{ds} = \int (V_{ds} - R_s i_{ds}) dt \quad (5)$$

Where the direct and quadrature axis components are obtain from the abc variables by using the transformation,

$$i_{qs} = i_{as} \quad (6)$$

$$i_{ds} = \frac{i_{cs} - i_{bs}}{\sqrt{3}} \quad (7)$$

### Voltage Source Inverter Fed Induction Motor Drives

The two basic voltage inverter fed induction motor systems are the pulse width modulated (PWM) inverter and the six step voltage source inverter (VSI) fed drives. The input converter is usually a diode bridge rectifier, which provides a constant dc voltage. After that a regenerative circuit is used which performs motor drive control and regenerative control. The dc voltage is filtered by a capacitor, which also provides a portion of the reactive current required by the inductive characteristics of an induction motor load. The filtered dc voltage is inverted by the PWM to provide the variable voltage and variable frequency ac output. Variable output voltage is achieved by pulse width modulation of the constant filtered dc bus voltage, which is the basic for the drive name.

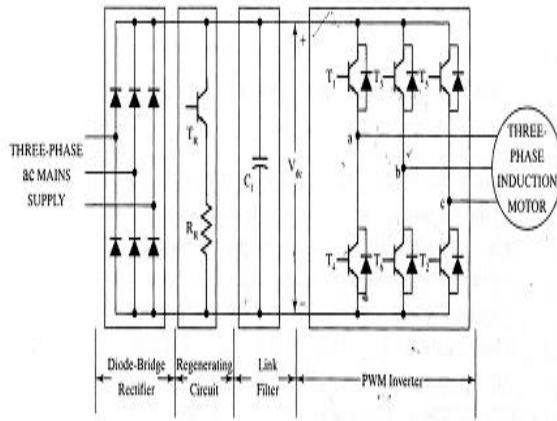


Figure 2: Power-Circuit Configuration of the Induction Motor Drive

Table 1: Inverter Switching States and Machine Voltages

States	$S_a$	$S_b$	$S_c$	$V_a$	$V_b$	$V_c$	$V_{ab}$	$V_{bc}$	$V_{ca}$	$V_{\alpha}$	$V_{\beta}$	$V_{\gamma}$	$V_{\delta}$
I	1	0	0	$V_{dc}$	0	0	$V_{dc}$	0	$-V_{dc}$	$\frac{2}{3}V_{dc}$	$-\frac{1}{3}V_{dc}$	$-\frac{1}{3}V_{dc}$	$\frac{2}{3}V_{dc}$
II	1	0	1	$V_{dc}$	0	$V_{dc}$	$-V_{dc}$	0	$\frac{1}{3}V_{dc}$	$-\frac{2}{3}V_{dc}$	$\frac{1}{3}V_{dc}$	$\frac{1}{3}V_{dc}$	$\frac{V_{dc}}{\sqrt{3}}$
III	0	0	1	0	0	$V_{dc}$	0	$-V_{dc}$	$\frac{1}{3}V_{dc}$	$\frac{1}{3}V_{dc}$	$\frac{2}{3}V_{dc}$	$-\frac{1}{3}V_{dc}$	$\frac{V_{dc}}{\sqrt{3}}$
IV	0	1	1	0	$V_{dc}$	$V_{dc}$	$-V_{dc}$	0	$V_{dc}$	$-\frac{2}{3}V_{dc}$	$\frac{1}{3}V_{dc}$	$\frac{1}{3}V_{dc}$	$-\frac{2}{3}V_{dc}$
V	0	1	0	0	$V_{dc}$	0	$-V_{dc}$	$V_{dc}$	$-\frac{1}{3}V_{dc}$	$\frac{2}{3}V_{dc}$	$-\frac{1}{3}V_{dc}$	$-\frac{1}{3}V_{dc}$	$-\frac{V_{dc}}{\sqrt{3}}$
VI	1	1	0	$V_{dc}$	$V_{dc}$	0	0	$V_{dc}$	$-V_{dc}$	$\frac{1}{3}V_{dc}$	$\frac{1}{3}V_{dc}$	$-\frac{2}{3}V_{dc}$	$\frac{V_{dc}}{\sqrt{3}}$
VII	0	0	0	0	0	0	0	0	0	0	0	0	0
VIII	1	1	1	$V_{dc}$	$V_{dc}$	$V_{dc}$	0	0	0	0	0	0	0

And machine phase voltages for a balanced system are

$$V_{as} = \frac{(V_{ab} - V_{ca})}{3}$$

$$V_{bs} = \frac{(V_{bc} - V_{ab})}{3} \quad (8)$$

$$V_{cs} = \frac{(V_{ca} - V_{bc})}{3}$$

And the stator q and d voltages for each phase are

$$V_{qs} = V_{as}$$

$$V_{ds} = \frac{1}{\sqrt{3}}(V_{cs} - V_{ds}) = \frac{1}{\sqrt{3}}V_{cb} \quad (9)$$

### Flux control

A uniform rotating stator flux is desirable, and it occupies one of the sextants (in the phasor diagram shown in Fig. 3) at any time. The stator flux phasor has a magnitude of  $\lambda_s$ , with an instantaneous position of  $\theta_{fs}$ . The corresponding d and q axes components are  $\lambda_{ds}$  and  $\lambda_{qs}$ , respectively.

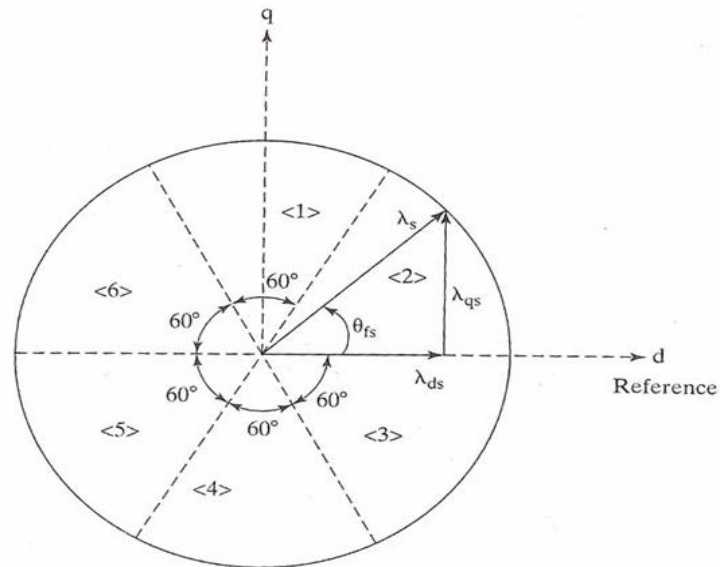


Figure 3: Division of Sextant for Stator Flux-Linkages Identification

### Torque Control

Torque control is exercised by comparison of the command torque to the torque measured from the stator flux linkages and stator currents as

$$T_e = \frac{3P}{2} (\lambda_{ds} i_{qs} - \lambda_{qs} i_{ds}) \quad (10)$$

The error torque is processed through a window comparator to procedure digital outputs,  $S_T$ , as follows as given in the table 2.

**Table 2: Generation of  $S_T$**

Condition	$S_T$
$(T_e^* - T_e) > \delta T_e$	1
$-\delta T_e < (T_e^* - T_e) < \delta T_e$	0
$(T_e^* - T_e) < -\delta T_e$	-1

Combining the flux error output  $S_\lambda$ , the torque error output  $S_T$ , and the sextant of the phasor  $S_\theta$  a switching table can be realized to obtain the switching states of the inverter, and it is given in Table 3.

**Table 3: Switching states for possible  $S_\lambda$ ,  $S_T$ , and  $S_\theta$**

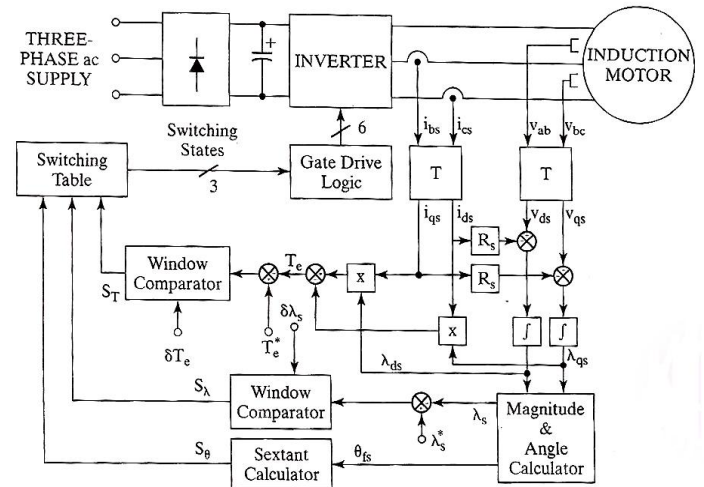
$S_\lambda$	$S_T$	$S_\theta$					
		<1>	<2>	<3>	<4>	<5>	<6>
1	1	VI	I	II	III	IV	V
1	0	VIII	VII	VIII	VII	VIII	VII
1	-1	II	III	IV	V	VI	I
0	1	V	VI	I	II	III	IV
0	0	VII	VIII	VII	VIII	VII	VIII
0	-1	III	IV	V	VI	I	II

### DTC Schematic

The following assumption are made for simplification,

1. The machine is linear i.e. saturation in the magnetic circuit is disregarded.
2. The air gap of the machine is uniform and the electromagnetic field is sinusoidal distributed i.e. the effect of space harmonic and their effect on torque and induced voltages is neglected.
3. Parameter of the machine remain constant

The damping coefficient associated with the mechanical rotational system of the machine and mechanical load is neglected.



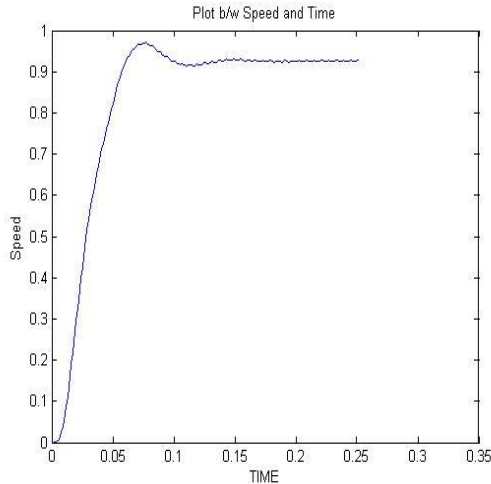
**Figure 4: Block diagram schematic of the direct torque (self) induction motor drive**

### Simulations and Results

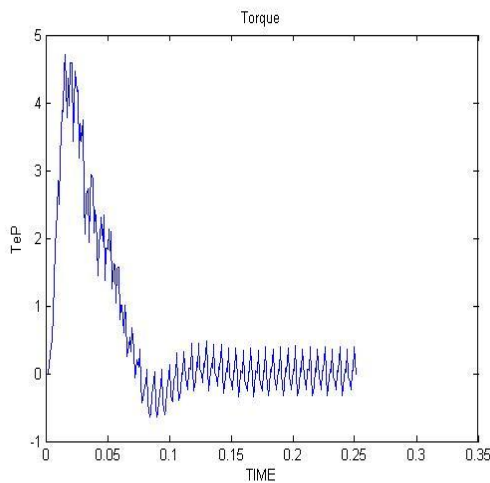
For the scheme  $R_r, L_s, L_r, L_m, J, P, T_{load}$  used for initialization, are as given in the Appendix A. The MATLAB code has been written for implementation of DTC for the induction motor model taken from [1]. The mathematical model consists of differential equations in terms of machine and motor parameters. The main parts of the direct torque control of induction motor are induction motor, voltage source inverter (VSI) and the functional blocks like adaptive

motor model, hysteresis controller and optimum pulse selector.

After tuning the PI controller gains the various response curves of the induction motor drive system for the combinations  $K_p L=0.020$ ,  $K_i L=0.06$ ,  $T=0.01$  are shown below



**Figure 5: Plot between Speed and time**



**Figure 6: Plot between Torque and time**

## Appendix A

Motor specifications: Power rating 5 HP, Max. Voltage 200 volt, Frequency 60 Hz, Stator resistance 0.183  $\Omega$ , Rotor resistance 0.277  $\Omega$ , Mutual inductance 0.0538 H, Stator self-inductance 0.0553 H, Rotor self inductance 0.05606 H, Number of poles 4, Moment of inertia 0.01667  $\text{kg}\cdot\text{m}^2$ .

The motor is at standstill. A set of balanced three-phase voltages at 70.7% of rated values at 60 Hz is applied.

## References

- [1] R. Krishnan, "Electric Motor Drives- Modeling, analysis and control." 2001 by Prentice-Hall.
- [2] T.G. Habetler, F. Profumo, M. Pastorelli, and L.M. Tolbert, "Direct Torque Control of Induction Machines using Space Vector Modulation." IEEE Trans. Industry Applications. Vol. 28, No. 5, Sept/Oct 1992, pp. 1045-1054.
- [3] P. Vas, "Sensorless Vector and Direct Torque Control", Oxford Univ. Press, Oxford, U.K., 1st edition, 1998.
- [4] C. Lascu, I. Boldea and F. Blbjerg, "A Modified Direct Torque Control for Induction Motor Sensorless Drive", IEEE Trans. On Industrial Application, Jan/Feb. 1998, Vol. 36, no.1, pp. 122-130.
- [5] I. Boldea and S.A. Nasar, "Electric Drives", CRC press, New York, 1<sup>st</sup> edition, 1999.
- [6] A. Purcell and P.P. Acarnley, "Enhanced Inverter Switching for Fast Response Direct Torque control", IEEE Trans. on power electronics, May 2001, Vol. 16, no.3, pp. 382-389.
- [7] G.K. Singh, "A Research Survey of Induction Motor Operation with Non-Sinusoidal Supply Wave Forms", Science Direct Trans. Electric Power System Research, 2005, Vol. 75, pp. 200-213.
- [8] Yuttana Kumsuwan, Suttichai Premrudeepreechacharn, Hamid A. Toliyat, "Modified Direct Torque Control Method for Induction Motor Drives Based on

- Amplitude and Angle Control of Stator Flux”, Science Direct Trans. Electric Power System Research, 2008, Vol. 78, pp. 1712-1718.
- [9] Yen-Shin Lai, “New Hybrid Fuzzy Controller for Direct Torque Control Induction Motor Drives”, IEEE Trans. on Power Electronics, Sept. 2003, Vol. 18, no. 5, pp. 1211-1219.
- [10] Rintu Khanna, Manish Singla and Gurpreet Kaur, “Fuzzy Logic Based Direct Torque Control of Induction Motor”, IEEE Trans. on Power Electronics, 2009, Vol. 978, no. 1, pp. 1-5.
- [11] K. L. Shi, T. F. Chan, Y. K. Wong and S. L. H, “Modelling and Simulation of the Three-Phase Induction Motor using Simulink”, Int. J. Elect. Engg. Edu, Printed in Great Britain, 1999, Vol. 36, pp. 163-172.
- [12] Shahriyar Kaboli, Esmaeel Vahdati-Khajeh, and Mohammad Reza Zolghadri, “Probabilistic Voltage Harmonic Analysis of Direct Torque Controlled Induction Motor”, IEEE Trans. on Power Electronics Drives, July 2006, Vol. 21, no.4, pp.1041-1052.